## PROBLEM SOLVING

Set C

Solutions
There are many commercial resources available to challenge students to become better problem solvers. This is a collection of some of our favorite problems.

You might consider allowing students to work with partners. Many of these problems are best solved with calculators. All of these problems lend themselves to students telling and writing about their thinking.

Consider expanding this problem solving deck by adding your own problems on the backs of the cards or photocopying the blank master we have included for you.

We hope you will share your great problems with us. Send them to :

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1) Answers will vary.
2) $\$ 3.75$ unless he is allowed to pay the 6 hr . rate

3) One possible solution:

Fold the 3 and 6 panel behind the 4 and 5 panel. Then fold the top half forward, over the bottom half.
Now fold the 3 panel to right over the middle panel and the right side over the middle. Turn the packet over and the numbers are in order!
6) Answers will vary.
7) Answers will vary.
8) 45

Segments:
AB, AC, AD, AE , AF
BC, BD, BE, BF
CD, CE, CF
DE, DF
EF
Yes, they are related. The principle involved is the number of combinations of N things taken M at a time. In the first case number of combinations of ten people taken 2 at a time. In the second case, the number of combinations of six points taken 2 at a time.
9) Answers will vary. Yes, the sum will be 18 .
10) .5 meter
11) Grades 5 and 6 may wish to cut out the figure and discover the relationships between the components, i.e. the combined area of the four small, white triangles $(A)=$ the area of the small black square(B). The area of the four large, black triangles is equal to $\mathrm{A}+\mathrm{B}$ or C . The area of the four large, white triangles is equal to $\mathrm{A}+\mathrm{B}+\mathrm{C}$ or D .

$$
\begin{aligned}
& A=50 \text { square } \mathrm{cm} ; B=50 \text { square } \mathrm{cm} ; \\
& C=100 \text { square } \mathrm{cm} ; D=200 \text { square } \mathrm{cm}
\end{aligned}
$$

Grades 6 and 7 and should use the Pythagorean relationship to arrive at similar conclusions.
12) Note 0.8 cents is a part of one cent or $\$ 0.008$

| Coin | No. in $\$ \mathbf{5}$ | Cost for $\mathbf{1}$ | Total Cost |
| :--- | :---: | :--- | :--- |
| penny | 500 | 0.008 | $\$ 4.00$ |
| nickel | 100 | 0.029 | $\$ 2.90$ |
| dime | 50 | 0.017 | $\$ 0.85$ |
| quarter | 20 | 0.037 | $\$ 0.74$ |
| half- | 10 | 0.078 | $\$ 0.78$ |
| dollar |  |  |  |

13) If the month has 31 days $\mathbf{1}$ will appear 14 times and 2 will appear 13 times.

If the month has 30 days $\mathbf{1}$ and $\mathbf{2}$ appear an equal number of times - 13 .

If February has 28 days then $\mathbf{1}$ appears 13 times and $\mathbf{2}$ appears 12 times. In leap years, $\mathbf{1}$ and $\mathbf{2}$ appear an equal number of times - 13 .
14) If it is digital, no contest - when it doesn't work it is blank! For an analog clock, to lose a minute an hour means it is right once and then not again for 720 hours. One minute's loss an hour x 60 makes it one hour behind. In the passage of 720 hours the clock will be 12 hours behind or right again! On the other hand a brocken clock is right twice a day.
15) Answers will vary. One-sixth is brown.
16) Answers will vary.
17) Answers will vary.
18) Four will have 4 blue faces and three will have 5 blue faces and one will have 3 blue faces.
19) $4,10,16,22,28,34,40,46,52,58$
$9,18,27,36,45,54,63,72,81,90$
20) Wednesday is the 21 st; the 17 th is a Saturday; February 14th is also a Wednesday.
21) Nine minutes or Never! After 9 minutes he is 0.1953125 feet away or alittle over 2 inches from the tree.
22)

23) $b$ is 100 th; 12 if the pattern is doubling.
24) 48
25) 220; 163
26)


27) Open all four links in one short chain. Use three of the open links to join the other three short chains. Now the last open link can join the ends for a continuous necklace.
Cost: 4 openings @ $\$ 3.00$ each +4 closings at $\$ 4.00$ each $=\$ 28.00$.
28) 9; yes, 6 .
29) $\$ 20.00$ profit.
30) 45 cubes; \# of cubes \# of painted faces

| 0 | 6 |
| :--- | :--- |
| 0 | 5 |
| 0 | 4 |
| 8 | 3 |
| 20 | 2 |
| 14 | 1 |
| 3 | 0 |

31) 13 go-carts, 17 tricycles.
32) 72 minutes.
33) Rosa has seven nickels.
34) 3/30/90; 5/18/90; 9/10/90; 10/9/90.

Bastille Day (7/14) and Christmas Eve (12/24) are equivalent to $1 / 2$. Ten other dates $1 / 2 ; 2 / 4$; 3/6; 4/8; 5/10; 6/12; 8/16; 9/18; 10/20; 11/22 fit this pattern.
35) $1+3+5+7+\ldots+13+15+17=$ ?


There are $41 / 2$ of these "pairs" so the sum is $4.5 \times 18$ or 81 .


There are 14 "pairs" or $14 \times 144=2016$.
36) $8 / 20 ; 1+2+3+4+5+6+7+8 \times 9$. Order of operations!
37) Thirteen. When 12 are in the group each could have unique birth months, but a 13th person will have a birth month that matches one of the other persons.
38) Answers will vary.
39) Ten

40) Answers will vary

Twelve tacks. If the edges overlap slightly the following array will work:

41) 120 outfits
42) Six hours - $\$ 1.26$

Ten hours - \$20.46
Eight hours for at least $\$ 5.00$
43) Bob-1, Rick - 9, Maria - 8 .
44) Sixth number - 40 .

No. The number of tests taken is needed.
45) Answers will vary. Here are some:

| \#right x 10 | - | \# wrong x 1 | $=\underline{\text { Score }}$ |
| :---: | :---: | :---: | :---: |
| $5 \times 10$ | - | $5 \times 1$ | $=45$ |
| $6 \times 10$ | - | $15 \times 1$ | $=45$ |
| $7 \times 10$ | - | $25 \times 1$ | $=45$ |
| $8 \times 10$ | - | $35 \times 1$ | $=45$ |
| $9 \times 10$ | - | $45 \times 1$ | $=45$ |
| $10 \times 10$ | - | $55 \times 1$ | $=45$ |

etc.
46) Average speed is Total Miles

Total Time

Time $=\underline{\text { Distance }}$
Speed
to the mountains: $\quad 600 \div 50=12$
from the mountains: $600 \div 55=10.90 \overline{90}$

So, average speed is $\frac{600+600}{12+10.90 \overline{90}}$ or $\sim 58.381$ miles per hour.

Since Distance = Rate x Time, you will need to know two of the quantities to solve future problems.
47) $6,8,12,16,24,32,48,96$ all divide 100 and have a remainder 4.96 is the largest. $10,14,15,21,30,35,42,70,105$ all divide 216 and have a remainder 6 .
48) Yes. Year born Age in Year

| 1 | 1 | 1 |
| :--- | :--- | :--- |
| 2 | 2 | 4 |
| 6 | 3 | 9 |
| 12 | 4 | 16 |
| 20 | 5 | 25 |
| 30 | 6 | 36 |


49) $85,86,87,88,89,90$
50) Eight days.
51) Answers will vary. Here's one:

52) Nine feet.
53) Answers will vary.
54) Just one 768. Answers should relate to the fact that if a number is divisible by nine then the sum of its digits is divisible by nine.
55) Condition 1: 33 numbers

| $0-100$ | 11 |
| :---: | :---: |
| $101-200$ | 11 |
| $201-300$ | 11 |

Condition 2: 24 numbers

| $0-100$ | 8 |
| :---: | :---: |
| $101-200$ | 8 |
| $201-300$ | 8 |

Condition 3: 27 numbers

$$
0-100 \quad 9
$$

$$
\text { 101-200 } 9
$$

201-300

$$
9
$$

56) 


perimeter 194 ft ; area of sidewalk $1020 \mathrm{sq} . \mathrm{ft}$.
57) Three ; $(2,5,5)$ isosceles, $(3,4,5)$ right,
$(4,4,4)$ equilateral.
58) Area: $\sim 71415.9$ square feet

Perimeter: ~1 028.3 feet
59) 1) 8 ; 2) 12 ; 3) 6 ; 4) 1 ; 5) 54
60) A. 40 pennies, 2 dimes, and 8 nickels $=\$ 1.00$
B. Answers will vary.
61) Yes. See answer to card 37
62) 800 letters by the 100 th week; 500 letters by the 63 rd week.

| Letters <br> Week Number |  | Letters <br> received |
| :--- | :--- | :--- |
| 1 | 8 | 8 |
| 2 | 8 | 16 |
| 3 | 8 | 24 |
| 4 | 8 | 32 |
| 5 | 8 | 40 |
| 6 | 8 | 48 |
| 7 | 8 | 56 |
| 8 | 8 | 64 |

63) $\$ 0.31$
